

```
1: #include "means.h"
2: #include <vector>
3: #include <iostream>
4: using namespace std;
5:
6: int main(int argc, char **argv)
7: {
8:     double arithmetic_mean, geometric_mean, harmonic_mean;
9:
10:    // Fixed version
11:    calculate_means(1, 4, 16, arithmetic_mean, geometric_mean, harmonic_mean);
12:    cout << arithmetic_mean << ", " << geometric_mean << ", " << harmonic_mean << endl;
13:
14:    calculate_means(2, 3, 5, arithmetic_mean, geometric_mean, harmonic_mean);
15:    cout << arithmetic_mean << ", " << geometric_mean << ", " << harmonic_mean << endl;
16:
17:    calculate_means(1000, 4000, 16000, arithmetic_mean, geometric_mean, harmonic_mean);
18:    cout << arithmetic_mean << ", " << geometric_mean << ", " << harmonic_mean << endl;
19:    cout << "-----" << endl;
20:
21:
22:
23:    // Scalable version
24:    calculate_means(vector<int> {1, 4, 16}, arithmetic_mean, geometric_mean, harmonic_mean);
25:    cout << arithmetic_mean << ", " << geometric_mean << ", " << harmonic_mean << endl;
26:
27:    calculate_means(vector<int> {2, 3, 5}, arithmetic_mean, geometric_mean, harmonic_mean);
28:    cout << arithmetic_mean << ", " << geometric_mean << ", " << harmonic_mean << endl;
29:
30:    calculate_means(vector<int> {1000, 4000, 16000}, arithmetic_mean, geometric_mean, harmonic_mean);
31:    cout << arithmetic_mean << ", " << geometric_mean << ", " << harmonic_mean << endl;
32:
33:
34:    return 0;
35: }
```

```
1: #include "../ex1A_mean_values/means.h"
2: #include <cmath>
3: #include <vector>
4:
5: void calculate_means(int a, int b, int c, double &am, double &gm, double &hm)
6: {
7:     am = (a + b + c)/3.0;
8:     gm = exp((log(a)+log(b)+log(c))/3); ✓
9:     hm = 3.0/(1.0/a + 1.0/b + 1.0/c);
10: }
11:
12: void calculate_means(std::vector<int> numbers, double &am, double &gm, double &hm)
13: {
14:     int n = numbers.size();
15:
16:     am = 0.;
17:     gm = 0.;
18:     hm = 0.;
19:
20:     for (int i = 0; i < n; ++i)
21:     {
22:         am += numbers[i];
23:         gm += log(numbers[i]); ✓
24:         hm += 1.0/numbers[i];
25:     }
26:
27:     am /= n;
28:     gm = exp(gm/n);
29:     hm = n/hm;
30: }
```

```
1: #pragma once
2: #include <vector>
3:
4: /**
5:  This function calculates arithmetic mean, geometric mean and harmonic mean of three integers.
6:  @param[in]    a          first integer
7:  @param[in]    b          second integer
8:  @param[in]    c          third integer
9:  @param[out]   am         arithmetic mean
10: @param[out]   gm         geometric mean
11: @param[out]   hm         harmonic mean
12: */
13: void calculate_means(int a, int b, int c, double &am, double &gm, double &hm);
14:
15: /**
16:  This function calculates arithmetic mean, geometric mean and harmonic mean of an integer vector.
17:  @param[in]    numbers    vector containing integers
18:  @param[out]   am         arithmetic mean
19:  @param[out]   gm         geometric mean
20:  @param[out]   hm         harmonic mean
21: */
22: void calculate_means(std::vector<int> numbers, double &am, double &gm, double &hm);
23:
```

```
1: #include "../ex1A_mean_values/means.h"
2: #include <iostream>
3: #include <fstream>
4: #include <cmath>
5: #include <vector>
6: #include <algorithm>
7: using namespace std;
8:
9:
10: int main(int argc, char **argv)
11: {
12:     // read vector from file
13:     vector<int> data_vector = {};
14:
15:     ifstream input_stream("data_1.txt");
16:
17:     int line;
18:     while(input_stream >> line)
19:     {
20:         data_vector.push_back(line);
21:     }
22:     data_vector.shrink_to_fit();
23:
24:
25:     // calculate minimum and maximum
26:     vector<int>::iterator min_it = min_element(data_vector.begin(), data_vector.end(
));
27:     vector<int>::iterator max_it = max_element(data_vector.begin(), data_vector.end(
));
28:
29:     // calculate arithmetic mean, geometric mean and harmonic mean
30:     double am, gm, hm;
31:     calculate_means(data_vector, am, gm, hm);
32:
33:
34:     // calculate standard deviation
35:     double sd = 0.;
36:     int n = data_vector.size();
37:     for (int i = 0; i < n; ++i)
38:     {
39:         sd += pow(data_vector[i] - am, 2);
40:     }
41:     sd = sqrt(sd/n);
42:
43:
44:     // print results
45:     cout << "minimum: " << *min_it << endl;
46:     cout << "maximum: " << *max_it << endl;
47:     cout << "arithmetic mean: " << am << endl;
48:     cout << "geometric mean: " << gm << endl;
49:     cout << "harmonic mean: " << hm << endl;
50:     cout << "standard deviation: " << sd << endl;
51:
52:     return 0;
53: }
```



```
1: #include "special_sum.h"
2: #include "../utils/timing.h"
3: #include <iostream>
4: #include <chrono>
5: #include <stack>
6: using namespace std;
7:
8: int main(int argc, char **argv)
9: {
10:     // check results and compare speeds
11:     for(size_t n : {15, 1001, 1432987})
12:     {
13:         cout << "n = " << n << endl;
14:         size_t sum_1, sum_2;
15:
16:         tic();
17:         for(size_t i = 0; i < 1000; ++i)
18:             sum_1 = special_sum_loop(n);
19:         double time_1 = toc();
20:
21:         tic();
22:         for(size_t i = 0; i < 1000; ++i)
23:             sum_2 = special_sum_noloop(n);
24:         double time_2 = toc();
25:
26:         cout << "loop: " << sum_1 << "\t\tDuration: " << time_1 << endl;
27:         cout << "no loop: " << sum_2 << "\t\tDuration: " << time_2 << endl << "-----"
-----" << endl;
28:     }
29:
30:     return 0;
31: }
```

```
1: #include "special_sum.h"
2:
3: size_t gauss_sum(size_t n)
4: {
5:     return (n*(n+1))/2;
6: }
7:
8: size_t special_sum_loop(size_t n)
9: {
10:     size_t sum = 0;
11:     for (size_t i = 1; i < n+1; ++i)
12:     {
13:         if (i % 3 == 0 || i % 5 == 0)
14:         {
15:             sum += i;
16:         }
17:     }
18:     return sum;
19: }
20:
21: size_t special_sum_noloop(size_t n)
22: {
23:     size_t factor_3 = gauss_sum(n/3);    // dividing int by int automatically gets rounded off
24:     size_t factor_5 = gauss_sum(n/5);
25:     size_t factor_15 = gauss_sum(n/15);
26:
27:     return factor_3*3 + factor_5*5 - factor_15*15;
28: }
```



```
1: #include <stddef>
2:
3: /**
4:  This function returns the sum of all positive integers less or equal n which are a
multiples of 3 or of 5, WITH using a loop.
5:  @param[in]    n
6:  @param[out]   M
7:  */
8: size_t special_sum_loop(size_t n);
9:
10:
11: /**
12:  This function returns the sum of all positive integers less or equal n which are a
multiples of 3 or of 5, WITHOUT using a loop.
13:  Example: For n=15, we have 60 = 3+5+6+9+10+12+15 = (1+2+3+4+5)*3 + (1+2+3)*5 - 1*1
5
14:  Formula:  $M = (\sum_{i=1}^{k_3} i) * 3 + (\sum_{i=1}^{k_5} i) * 5 - (\sum_{i=1}^{k_{15}} i) * 15$ 
15:  @param[in]    n
16:  @param[out]   M
17:  */
18: size_t special_sum_noloop(size_t n);
```

```
1: #include "mylib.h"
2: #include <cmath>
3: #include <iostream>
4: using namespace std;
5:
6: int main(int argc, char **argv)
7: {
8:     for(size_t i = 1; i < 8; ++i)
9:     {
10:         size_t n = pow(10,i);
11:         vector<double> x(n);
12:         for (size_t k = 0; k < n; ++k)
13:             x[k] = 1.0/(k + 1);
14:
15:
16:         // compute scalar products
17:         double sum_1 = scalar(x, x);
18:         double sum_2 = Kahan_skalar(x, x);
19:
20:         // compute error
21:         double err_1 = abs(sum_1 - pow(M_PI,2)/6);
22:         double err_2 = abs(sum_2 - pow(M_PI,2)/6);
23:
24:         cout << "n = " << n << endl;
25:         cout << "Normal scalar product: " << sum_1 << "\terror: " << err_1 << endl;
26:         cout << "Kahan scalar product: " << sum_2 << "\terror: " << err_2 << endl;
27:         cout << endl;
28:     }
29:
30:
31:
32:     return 0;
33: }
```

```
1: #include "mylib.h"
2: #include <cassert>           // assert()
3: #include <cmath>
4: #include <vector>
5: using namespace std;
6:
7: double scalar(vector<double> const &x, vector<double> const &y)
8: {
9:     assert(x.size() == y.size());
10:    size_t const N = x.size();
11:    double sum = 0.0;
12:    for (size_t i = 0; i < N; ++i)
13:    {
14:        sum += x[i] * y[i];
15:    }
16:    return sum;
17: }
18:
19:
20:
21: double Kahan_skalar(vector<double> const &x, vector<double> const &y)
22: {
23:     double sum = 0;
24:     double c = 0;
25:     size_t n = x.size();
26:     for (size_t i = 0; i < n; ++i)
27:     {
28:         double z = x[i]*y[i] - c;    // c is the part that got lost in the last iteration
29:         double t = sum + z;          // when adding sum + z, the lower digits are lost if sum is large
30:         c = (t - sum) - z;           // now we recover the lower digits to add in the next iteration
31:         sum = t;
32:     }
33:     return sum;
34: }
```



```
1: #ifndef FILE_MYLIB
2: #define FILE_MYLIB
3: #include <vector>
4:
5: /**      Inner product
6:      @param[in] x      vector
7:      @param[in] y      vector
8:      @return           resulting Euclidian inner product <x,y>
9: */
10: double scalar(std::vector<double> const &x, std::vector<double> const &y);
11:
12: /**      Inner product using BLAS routines
13:      @param[in] x      vector
14:      @param[in] y      vector
15:      @return           resulting Euclidian inner product <x,y>
16: */
17: double scalar_cblas(std::vector<double> const &x, std::vector<double> const &y);
18: float scalar_cblas(std::vector<float> const &x, std::vector<float> const &y);
19:
20:
21: /**      L_2 Norm of a vector
22:      @param[in] x      vector
23:      @return           resulting Euclidian norm <x,y>
24: */
25: double norm(std::vector<double> const &x);
26:
27: double Kahan_skalar(std::vector<double> const &x, std::vector<double> const &y);
28:
29:
30: #endif
```

```
1: #include "../utils/timing.h"
2: #include <iostream>
3: #include <random>
4: #include <chrono>
5: #include <vector>
6: #include <list>
7: #include <algorithm>
8: using namespace std;
9:
10:
11: size_t random_integer(int lower_bound, int upper_bound)
12: {
13:     unsigned seed = chrono::system_clock::now().time_since_epoch().count();
14:
15:     minstd_rand0 generator (seed);
16:
17:     return lower_bound + generator() % (upper_bound - lower_bound + 1);
18: }
19:
20: int main(int argc, char **argv)
21: {
22:     // start with generating a sorted vector/list
23:     size_t n = 10000;
24:     vector<int> x_vec = {};
25:     list<int> x_list = {};
26:     for(size_t k = 0; k < n; ++k)
27:     {
28:         x_vec.push_back(k + 1);
29:         x_list.push_back(k + 1);
30:     }
31:
32:
33:     // insert new random entries such that the container stays sorted
34:     tic();
35:     for(size_t i = 0; i < n; ++i)
36:     {
37:         size_t new_entry = random_integer(1,n);
38:         auto it = lower_bound(x_vec.begin(), x_vec.end(), new_entry);
39:         x_vec.insert(it, new_entry);
40:     }
41:     double time_1 = toc();
42:
43:     tic();
44:     for(size_t i = 0; i < n; ++i)
45:     {
46:         size_t new_entry = random_integer(1,n);
47:         auto it = lower_bound(x_list.begin(), x_list.end(), new_entry);
48:         x_list.insert(it, new_entry);
49:     }
50:     double time_2 = toc();
51:
52:
53:     // check results
54:     cout << "New vector is sorted: " << std::boolalpha << is_sorted(x_vec.begin(), x_vec.end()) << "\tsize: " << x_vec.size() << "\tduration: " << time_1 << endl;
55:     cout << "New list is sorted: " << std::boolalpha << is_sorted(x_list.begin(), x_list.end()) << "\tsize: " << x_list.size() << "\tduration: " << time_2 << endl;
56:
57:
58:     return 0;
59: }
```

```
1: #include "goldbach.h"
2:
3: size_t single_goldbach(size_t k)
4: {
5:     const std::vector<size_t> relevant_primes = get_primes(k);
6:     size_t m = relevant_primes.size();
7:
8:     size_t counter = 0;
9:
10:    for(size_t i = 0; i < m; ++i)
11:    {
12:        for(size_t j = i; j < m; ++j)
13:        {
14:            if(relevant_primes[i] + relevant_primes[j] == k)
15:                counter += 1;
16:        }
17:    }
18:
19:    return counter;
20: }
21:
22:
23: std::vector<size_t> count_goldbach(size_t n)
24: {
25:     const std::vector<size_t> relevant_primes = get_primes(n);
26:     size_t m = relevant_primes.size();
27:
28:     std::vector<size_t> counter_vector(n + 1, 0);
29:
30:
31:    for(size_t i = 0; i < m; ++i)
32:    {
33:        for(size_t j = i; j < m; ++j)
34:        {
35:            size_t sum = relevant_primes[i] + relevant_primes[j];
36:            if(sum <= n)
37:                ++counter_vector[relevant_primes[i] + relevant_primes[j]];
38:        }
39:    }
40:
41:    return counter_vector;
42: }
```



```
1: #pragma once
2: #include "mayer_primes.h"
3: #include <iostream>
4: #include <vector>
5: #include <iterator>
6: #include <cassert>
7:
8:
9: /**
10:  This function returns the number of possible decompositions of an integer into a s
um of two prime numbers.
11:  @param[in]    k          first integer
12:  @param[out]   count      number of decompositions
13:  */
14: size_t single_goldbach(size_t k);
15:
16: /**
17:  This function returns the number of possible decompositions into a sum of two prim
e numbers of all even integers in the interval [4,n].
18:  @param[in]    n          upper integer bound
19:  @param[out]   count_vector  vector containing the number of decompositions f
or a natural number the corresponding index
20:  */
21: std::vector<size_t> count_goldbach(size_t n);
```

```
1: #include "../utils/timing.h"
2: #include "goldbach.h"
3: #include <iostream>
4: #include <algorithm>
5: using namespace std;
6:
7:
8: int main(int argc, char **argv)
9: {
10:     cout << "Check: 694 has " << single_goldbach(694) << " decompositions." << endl <
< "-----" << endl;
11:
12:
13:     for(size_t n : {10000, 100000, 400000, 1000000, 2000000})
14:     {
15:         tic();
16:
17:         auto goldbach_vector = count_goldbach(n);
18:
19:         auto max_it = max_element(goldbach_vector.begin(), goldbach_vector.end());
20:         size_t max_number = distance(goldbach_vector.begin(), max_it);
21:
22:         double time = toc();
23:
24:         cout << "The number " << max_number << " has " << *max_it << " decompositio
ns. Duration: " << time << endl;
25:     }
26:
27:     /*
28:     The number 9240 has 329 decompositions. Duration: 0.00572876
29:     The number 99330 has 2168 decompositions. Duration: 0.3342
30:     The number 390390 has 7094 decompositions. Duration: 4.23734
31:     The number 990990 has 15594 decompositions. Duration: 29.5817
32:     The number 1981980 has 27988 decompositions. Duration: 135.985
33:     */
34:
35:
36:     return 0;
37: }
```

```

1: #pragma once
2:
3: #include <cstring> //memset
4: #include <vector>
5: //using namespace std;
6:
7: /** \brief Determines all prime numbers in interval [2, @p max].
8:  *
9:  * The sieve of Eratosthenes is used.
10:  *
11:  * The implementation originates from <a href="http://code.activestate.com/recipes/
576559-fast-prime-generator/">Florian Mayer</a>.
12:  *
13:  * \param[in] max end of interval for the prime number search.
14:  * \return vector of prime numbers @f$2,3,5, \dots, p\leq\max @f$.
15:  *
16:  * \copyright
17:  * Copyright (c) 2008 Florian Mayer (adapted by Gundolf Haase 2018)
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TWARE.
35:  *
36:  */
37: template <class T>
38: std::vector<T> get_primes(T max)
39: {
40:     std::vector<T> primes;
41:     char *sieve;
42:     sieve = new char[max / 8 + 1];
43:     // Fill sieve with 1
44:     memset(sieve, 0xFF, (max / 8 + 1) * sizeof(char));
45:     for (T x = 2; x <= max; x++)
46:     {
47:         if (sieve[x / 8] & (0x01 << (x % 8))) {
48:             primes.push_back(x);
49:             // Is prime. Mark multiples.
50:             for (T j = 2 * x; j <= max; j += x)
51:             {
52:                 sieve[j / 8] &= ~(0x01 << (j % 8));
53:             }
54:         }
55:     }
56:     delete[] sieve;
57:     return primes;
58: }
59:
60: //-----
61: //int main() // by Florian Mayer
62: //{g++ -O3 -std=c++14 -fopenmp main.cpp && ./a.out
63: // vector<unsigned long> primes;
64: // primes = get_primes(10000000);
65: // // return 0;

```

```
66: //      // Print out result.
67: //      vector<unsigned long>::iterator it;
68: //      for(it=primes.begin(); it < primes.end(); it++)
69: //          cout << *it << " ";
70: //
71: //      cout << endl;
72: //      return 0;
73: //}
74:
```

```

1: #pragma once
2: #include "sigmoid.h"
3: #include <iostream>
4: #include <vector>
5: using namespace std;
6:
7: class DenseMatrix
8: {
9:     private:
10:         vector<double> M;
11:         size_t n;
12:         size_t m;
13:
14:
15:     public:
16:         vector<double> Mult(const vector<double> &x) const
17:         {
18:             vector<double> y(n,0);
19:             for(size_t i = 0; i < n; ++i)    // iterate row
20:             {
21:                 for(size_t j = 0; j < m; ++j)    // iterate column
22:                 {
23:                     y[i] += M[i*m + j]*x[j];
24:                 }
25:             }
26:             return y;
27:         }
28:
29:         vector<double> MultT(const vector<double> &y) const
30:         {
31:             vector<double> x(m,0);
32:             for(size_t j = 0; j < m; ++j)    // iterate column
33:             {
34:                 for(size_t i = 0; i < n; ++i)    // iterate row
35:                 {
36:                     x[j] += M[i*m + j]*y[i];
37:                 }
38:             }
39:             return x;
40:         }
41:
42:         void Print() const
43:         {
44:             for(size_t i = 0; i < n; ++i)    // iterate row
45:             {
46:                 for(size_t j = 0; j < m; ++j)    // iterate column
47:                 {
48:                     cout << M[i*m + j] << " ";
49:                 }
50:                 cout << endl;
51:             }
52:             cout << endl;
53:         }
54:
55:
56:         DenseMatrix(size_t n, size_t m)
57:         {
58:             this->n = n;
59:             this->m = m;
60:             M = vector<double>(n*m);
61:             size_t nm = max(n,m);
62:
63:             for(size_t i = 0; i < n; ++i)    // iterate row
64:             {
65:                 for(size_t j = 0; j < m; ++j)    // iterate column
66:                 {
67:                     M[i*m + j] = sigmoid(x_entry(i,nm))*sigmoid(x_entry(j,nm));
68:                 }

```

Access pattern

```
69:         }  
70:     }  
71: };
```

```

1: #include "../utils/timing.h"
2: #include "DenseMatrix.h"
3: #include "ProductMatrix.h"
4: #include <algorithm>
5:
6: int main()
7: {
8:     // b) -----
9:     DenseMatrix const M(5,3);
10:    vector<double> const u{{1, 2, 3}};
11:    vector<double> f1 = M.Mult(u);
12:    vector<double> const v{{-1, 2, -3, 4, -5}};
13:    vector<double> f2 = M.MultT(v);
14:
15:    M.Print();
16:
17:    for(size_t i = 0; i < f1.size(); ++i)
18:        cout << f1[i] << endl;
19:    cout << endl;
20:
21:
22:    for(size_t j = 0; j < f2.size(); ++j)
23:        cout << f2[j] << " ";
24:    cout << endl << "-----" << endl;
25:
26:    // c) -----
27:    size_t n = pow(10,3);
28:    DenseMatrix const M_1(n,n);
29:    vector<double> x(n, 1.0);
30:
31:    size_t n_loops = 100;
32:    vector<double> y_1;
33:    vector<double> y_2;
34:
35:    double time_1 = 0;
36:    double time_2 = 0;
37:
38:    tic();
39:    for(int l = 0; l < n_loops; ++l)
40:        y_1 = M_1.Mult(x);
41:    time_1 += toc();
42:
43:    tic();
44:    for(int l = 0; l < n_loops; ++l)
45:        y_2 = M_1.MultT(x);
46:    time_2 += toc();
47:
48:    vector<double> error_vec(n,0);
49:    for(int i = 0; i < n; ++i)
50:        error_vec[i] = abs(y_1[i] - y_2[i]);
51:    double sup_error = *max_element(error_vec.begin(), error_vec.end());
52:
53:
54:    cout << "n = " << n << endl;
55:    cout << "Average duration for Mult: " << time_1/n_loops << endl;
56:    cout << "Average duration for MultT: " << time_2/n_loops << endl;
57:    cout << "sup-error: " << sup_error << endl;
58:    cout << "-----" << endl;
59:
60:    // d) -----
61:    vector<double> u_M(n,0);
62:    for(int i = 0; i < n; ++i)
63:        u_M[i] = sigmoid(x_entry(i, n));
64:
65:    ProductMatrix const M_2(u_M, u_M);

```

```
66:
67:     time_1 = 0;
68:     time_2 = 0;
69:
70:     tic();
71:     for(int l = 0; l < n_loops; ++l)
72:         y_1 = M_2.Mult(x);
73:     time_1 += toc();
74:
75:     tic();
76:     for(int l = 0; l < n_loops; ++l)
77:         y_2 = M_2.MultT(x);
78:     time_2 += toc();
79:
80:     for(int i = 0; i < n; ++i)
81:         error_vec[i] = abs(y_1[i] - y_2[i]);
82:     sup_error = *max_element(error_vec.begin(), error_vec.end());
83:
84:
85:     cout << "n = " << n << endl;
86:     cout << "Average duration for Mult: " << time_1/n_loops << endl;
87:     cout << "Average duration for MultT: " << time_2/n_loops << endl;
88:     cout << "sup-error: " << sup_error << endl;
89:     cout << "-----" << endl;
90:
91:
92:     return 0;
93: }
```

```

1: #pragma once
2: #include <cmath>
3: #include <iostream>
4: #include <vector>
5: using namespace std;
6:
7: class ProductMatrix
8: {
9:     private:
10:         vector<double> u;
11:         vector<double> v;
12:         size_t n;
13:         size_t m;
14:
15:     public:
16:         vector<double> Mult(const vector<double> &x) const
17:         {
18:             vector<double> y(n,0);
19:             for(int i = 0; i < n; ++i)
20:             {
21:                 for(int j = 0; j < m; ++j)
22:                 {
23:                     y[i] += v[j]*x[j];
24:                 }
25:                 y[i] *= u[i];
26:             }
27:             return y;
28:         }
29:
30:         vector<double> MultT(const vector<double> &y) const
31:         {
32:             vector<double> x(m,0);
33:             for(int j = 0; j < m; ++j)
34:             {
35:                 for(int i = 0; i < n; ++i)
36:                 {
37:                     x[j] += y[i]*u[i];
38:                 }
39:                 x[j] *= v[j];
40:             }
41:             return x;
42:         }
43:
44:         ProductMatrix(const vector<double> &u, const vector<double> &v)
45:         {
46:             n = u.size();
47:             m = v.size();
48:             this->u = u;
49:             this->v = v;
50:         }
51:     };
52: };

```

$y_i = \text{scal} = \text{const} \quad \forall i$

$x_j = \text{scal} = \text{const} \quad \forall j$

```
1: #pragma once
2: #include <cmath>
3:
4: double sigmoid(double x)
5: {
6:     return 1./(1. + exp(-x));
7: }
8:
9: double x_entry(size_t k, size_t nm)
10: {
11:     return (10.*k)/(nm - 1) - 5.;
12: }
```

```

1: //
2: //      Gundolf Haase, Oct 18 2024
3: //
4: #pragma once
5:
6: #ifdef __NVCC__
7: #include <cuda_runtime.h>
8: #endif
9: #ifdef _OPENMP
10: #include <omp.h>
11: #endif
12: #include <iostream>
13: #include <unordered_map>
14:
15: #####
16: // G.Haase
17: // See https://sourceforge.net/p/predef/wiki/Compilers/
18: //      http://www.cplusplus.com/doc/tutorial/preprocessor/
19: // also: export OMP_DISPLAY_ENV=VERBOSE
20: #####
21: /**      Checks for compilers, its versions, threads etc. on CPU
22:  *
23:      @param[in] argc number of command line arguments
24:      @param[in] argv command line arguments as array of C-strings
25:  */
26: template <class T>
27: void check_env(T argc, char const *argv[])
28: {
29:     std::cout << "\n#####\n";
#####\n";
30:     std::cout << "Code      :";
31:     for (T k = 0; k < argc; ++k) std::cout << " " << argv[k];
32:     std::cout << std::endl;
33:
34:     // compiler:      https://sourceforge.net/p/predef/wiki/Compilers/
35:     std::cout << "Compiler: ";
36: #if defined __INTEL_COMPILER
37: #pragma message(" ##### INTEL #####")
38:     std::cout << "INTEL " << __INTEL_COMPILER;
39:     // Ignore warnings for #pragma acc unrecognized
40: #pragma warning disable 161
41:     // Ignore warnings for #pragma omp unrecognized
42: #pragma warning disable 3180
43:
44: #elif defined __NVCC__
45: // #pragma message(" ##### NVCC #####")
46: // https://docs.nvidia.com/cuda/cuda-compiler-driver-nvcc/
47:     std::cout << "NVCC " << __CUDACC_VER_MAJOR__ << "." << __CUDACC_VER_MINOR__ ;
48: #elif defined __clang__
49: #pragma message(" ##### CLANG #####")
50:     std::cout << "CLANG " << __clang_major__ << "." << __clang_minor__ << "."; // <<
__clang_patchlevel__;
51: #elif defined __GNUC__
52: // #pragma message(" ##### Gnu #####")
53:     std::cout << "Gnu " << __GNUC__ << "." << __GNUC_MINOR__ << "." << __GNUC_PATCH
HLEVEL__;
54: #else
55: #pragma message(" ##### unknown Compiler #####")
56:     std::cout << "unknown";
57: #endif
58:     std::cout << " C++ standard: " << __cplusplus << std::endl;
59:
60:     // Parallel environments
61:     std::cout << "Parallel: ";
62: #if defined MPI_VERSION
63: #ifndef __GNUC__
64: #pragma message(" ##### MPI #####")
65: #endif

```

```

66: #ifndef OPEN_MPI
67:     std::cout << "OpenMPI ";
68: #else
69:     std::cout << "MPI ";
70: #endif
71:     std::cout << MPI_VERSION << "." << MPI_SUBVERSION << " ";
72: #endif
73:
74: #ifdef _OPENMP
75: //https://www.openmp.org/specifications/
76: //https://stackoverflow.com/questions/1304363/how-to-check-the-version-of-openmp-on-
linux
77:     std::unordered_map<unsigned, std::string> const map{
78:         {200505, "2.5"}, {200805, "3.0"}, {201107, "3.1"}, {201307, "4.0"}, {201511,
"4.5"}, {201611, "5.0"}, {201811, "5.0"};
79: #ifndef __GNUC__
80: #pragma message(" ##### OPENMP #####")
81: #endif
82:     std::cout << "OpenMP ";
83:     try {
84:         std::cout << map.at(_OPENMP);
85:     }
86:     catch (...) {
87:         std::cout << _OPENMP;
88:     }
89:     #pragma omp parallel
90:     {
91:         #pragma omp master
92:         {
93:             const int nn = omp_get_num_threads(); // OpenMP
94:             std::cout << " ---> " << nn << " Threads ";
95:         }
96:         #pragma omp barrier
97:     }
98:
99: #endif
100: #ifdef _OPENACC
101: #pragma message(" ##### OPENACC #####")
102:     std::cout << "OpenACC ";
103: #endif
104:     std::cout << std::endl;
105:     std::cout << "Date : " << __DATE__ << " " << __TIME__;
106:     std::cout << "\n#####\n";
#####\n";
107: }
108:
109:
110:
111: /** @brief Lists basic properties of GPU
112: */
113: inline
114: void printGPUInfo()
115: {
116:     using std::cout, std::endl, std::boolalpha;
117: #ifdef __NVCC__
118:     cout << "\n++++++\n";
119:     // https://devblogs.nvidia.com/how-query-device-properties-and-handle-errors-cud
a-cc/
120:     int nDevices;
121:     cudaError_t err = cudaGetDeviceCount(&nDevices);
122:     if (err != cudaSuccess) printf("%i : %s\n", err, cudaGetErrorString(err));
123:
124:     // https://docs.nvidia.com/cuda/cuda-runtime-api/structcudaDeviceProp.html
125:     cudaDeviceProp prop;
126:     // https://www.cs.cmu.edu/afs/cs/academic/class/15668-s11/www/cuda-doc/html/grou
p_CUDART_DEVICE_g5aa4f47938af8276f08074d09b7d520c.html
127:     err = cudaGetDeviceProperties (&prop, 0);
128:     if (err != cudaSuccess) printf("%i : %s\n", err, cudaGetErrorString(err));

```

```
129:     cout << "We work on " << nDevices << " x " << prop.name << " GPU \n    with "
130:     << prop.multiProcessorCount << " Multiprocessors (SME)"
131:     << ", Compute capability " << prop.major << "." << prop.minor << endl;
132:     cout << "global Mem: " << prop.totalGlobalMem/1024/1000/1000 << " GB" << endl;
133:     cout << "shared Mem per SME: " << prop.sharedMemPerMultiprocessor/1024 << "kB"
134:     << "    shared Mem per Block: " << prop.sharedMemPerBlock/1024 << " kB"
135:     << "    32b-Registers per Block: " << prop.regsPerBlock << endl;
136:     cout << "global L2 cache: " << prop.l2CacheSize/1024 << " kB"
137:     << "    local L1 cache supported: " << boolalpha << bool(prop.localL1CacheSu
pported) << endl;
138:     cout << "max Threads per Block:" << prop.maxThreadsPerBlock << endl;
139:     cout << "+++++\n";
140: #else
141:     cout << endl << "No compiler support for GPU" << endl;
142: #endif
143: }
144:
145:
```

```
1: #include "timing.h" // tic(), toc()
2: #include "info.h"
3: #include "std_lib_facilities.h" // overload [] : by Stroustrup
4: #include <iostream>
5: using namespace std;
6:
7: int main(int argc , char const *argv[])
8: {
9:     cout << "Check my own headers\n" << endl;
10:
11:     tic(); // start timer
12:     check_env(argc, argv); // info on compiler
13:     printGPUInfo(); // info on GPU. Only in NVCC_
14:     double tt(toc()); // end timer
15:     cout << "\n\nSeconds: " << tt << endl;
16:
17:     vector<double> aa(5,-1.2345);
18:     try
19:     {
20:         cout << "\nThe next line should result in an exception\n";
21:         cout << aa[5] << endl; // Stroustrups overloading should check the index rang
22:     }
23:     catch (Range_error &re)
24:     {
25:         cout << "Index out of range!!!\n";
26:     }
27:
28:     return 0;
29: }
30:
```

e

```

1:  /*
2:  std_lib_facilities.h
3:  */
4:
5:  /*
6:  simple "Programming: Principles and Practice using C++ (second edition)" course head
er to
7:  be used for the first few weeks.
8:  It provides the most common standard headers (in the global namespace)
9:  and minimal exception/error support.
10:
11:  Students: please don't try to understand the details of headers just yet.
12:  All will be explained. This header is primarily used so that you don't have
13:  to understand every concept all at once.
14:
15:  By Chapter 10, you don't need this file and after Chapter 21, you'll understand it
16:
17:  Revised April 25, 2010: simple_error() added
18:
19:  Revised November 25 2013: remove support for pre-C++11 compilers, use C++11: <chrono
>
20:  Revised November 28 2013: add a few container algorithms
21:  Revised June 8 2014: added #ifndef to workaround Microsoft C++11 weakness
22:  Revised February 2 2015: randint() can now be seeded (see exercise 5.13).
23:  Revised August 3, 2020: a cleanup removing support for ancient compilers
24:  */
25:
26:  #ifndef H112
27:  #define H112 080315L
28:
29:
30:  #include<iostream>
31:  #include<iomanip>
32:  #include<fstream>
33:  #include<sstream>
34:  #include<cmath>
35:  #include<cstdlib>
36:  #include<string>
37:  #include<list>
38:  #include <forward_list>
39:  #include<vector>
40:  #include<unordered_map>
41:  #include<algorithm>
42:  #include <array>
43:  #include <regex>
44:  #include<random>
45:  #include<stdexcept>
46:
47:  //-----
48:
49:
50:  typedef long Unicode;
51:
52:  //-----
53:
54:  using namespace std;
55:
56:  template<class T> string to_string(const T& t)
57:  {
58:      ostringstream os;
59:      os << t;
60:      return os.str();
61:  }
62:
63:  struct Range_error : out_of_range {      // enhanced vector range error reporting
64:      int index;
65:      Range_error(int i) :out_of_range("Range error: " + to_string(i)), index(i) {
}

```

```

66: };
67:
68:
69: // trivially range-checked vector (no iterator checking):
70: template< class T> struct Vector : public std::vector<T> {
71:     using size_type = typename std::vector<T>::size_type;
72:
73:     /* #ifdef _MSC_VER
74:         // microsoft doesn't yet support C++11 inheriting constructors
75:         Vector() { }
76:         explicit Vector(size_type n) :std::vector<T>(n) {}
77:         Vector(size_type n, const T& v) :std::vector<T>(n, v) {}
78:         template <class I>
79:         Vector(I first, I last) : std::vector<T>(first, last) {}
80:         Vector(initializer_list<T> list) : std::vector<T>(list) {}
81:     */
82:     using std::vector<T>::vector;    // inheriting constructor
83:
84:     T& operator[](unsigned int i) // rather than return at(i);
85:     {
86:         if (/*i<0 || */ this->size() <= i) throw Range_error(i);
87:         return std::vector<T>::operator[](i);
88:     }
89:     const T& operator[](unsigned int i) const
90:     {
91:         if (/*i<0 || */ this->size() <= i) throw Range_error(i);
92:         return std::vector<T>::operator[](i);
93:     }
94: };
95:
96: // disgusting macro hack to get a range checked vector:
97: #define vector Vector
98:
99: // trivially range-checked string (no iterator checking):
100: struct String : std::string {
101:     using size_type = std::string::size_type;
102:     // using string::string;
103:
104:     char& operator[](unsigned int i) // rather than return at(i);
105:     {
106:         if (/*i<0 || */ size() <= i) throw Range_error(i);
107:         return std::string::operator[](i);
108:     }
109:
110:     const char& operator[](unsigned int i) const
111:     {
112:         if (/*i<0 || */ size() <= i) throw Range_error(i);
113:         return std::string::operator[](i);
114:     }
115: };
116:
117:
118: namespace std {
119:
120:     template<> struct hash<String>
121:     {
122:         size_t operator()(const String& s) const
123:         {
124:             return hash<std::string>()(s);
125:         }
126:     };
127:
128: } // of namespace std
129:
130:
131: struct Exit : runtime_error {
132:     Exit() : runtime_error("Exit") {}
133: };

```

```
134:
135: // error() simply disguises throws:
136: inline void error(const string& s)
137: {
138:     throw runtime_error(s);
139: }
140:
141: inline void error(const string& s, const string& s2)
142: {
143:     error(s + s2);
144: }
145:
146: inline void error(const string& s, int i)
147: {
148:     ostringstream os;
149:     os << s << ": " << i;
150:     error(os.str());
151: }
152:
153:
154: template<class T> char* as_bytes(T& i) // needed for binary I/O
155: {
156:     void* addr = &i; // get the address of the first byte
157:     // of memory used to store the object
158:     return static_cast<char*>(addr); // treat that memory as bytes
159: }
160:
161:
162: inline void keep_window_open()
163: {
164:     cin.clear();
165:     cout << "Please enter a character to exit\n";
166:     char ch;
167:     cin >> ch;
168:     return;
169: }
170:
171: inline void keep_window_open(string s)
172: {
173:     if (s == "") return;
174:     cin.clear();
175:     cin.ignore(120, '\n');
176:     for (;;) {
177:         cout << "Please enter " << s << " to exit\n";
178:         string ss;
179:         while (cin >> ss && ss != s)
180:             cout << "Please enter " << s << " to exit\n";
181:         return;
182:     }
183: }
184:
185:
186:
187: // error function to be used (only) until error() is introduced in Chapter 5:
188: inline void simple_error(string s) // write 'error: s and exit program
189: {
190:     cerr << "error: " << s << '\n';
191:     keep_window_open(); // for some Windows environments
192:     exit(1);
193: }
194:
195: // make std::min() and std::max() accessible on systems with antisocial macros:
196: #undef min
197: #undef max
198:
199:
200: // run-time checked narrowing cast (type conversion). See ???.
201: template<class R, class A> R narrow_cast(const A& a)
```

```
202: {
203:     R r = R(a);
204:     if (A(r) != a) error(string("info loss"));
205:     return r;
206: }
207:
208: // random number generators. See 24.7.
209:
210: inline default_random_engine& get_rand()
211: {
212:     static default_random_engine ran;           // note: not thread_local
213:     return ran;
214: };
215:
216: inline void seed_randint(int s) { get_rand().seed(s); }
217:
218: inline int randint(int min, int max) { return uniform_int_distribution<>(min, max)(g
et_rand()); }
219:
220: inline int randint(int max) { return randint(0, max); }
221:
222: //inline double sqrt(int x) { return sqrt(double(x)); } // to match C++0x
223:
224: // container algorithms. See 21.9. // C++ has better versions of this:
225:
226: template<typename C>
227: using Value_type = typename C::value_type;
228:
229: template<typename C>
230: using Iterator = typename C::iterator;
231:
232: template<typename C>
233: // requires Container<C>()
234: void sort(C& c)
235: {
236:     std::sort(c.begin(), c.end());
237: }
238:
239: template<typename C, typename Pred>
240: // requires Container<C>() && Binary_Predicate<Value_type<C>>()
241: void sort(C& c, Pred p)
242: {
243:     std::sort(c.begin(), c.end(), p);
244: }
245:
246: template<typename C, typename Val>
247: // requires Container<C>() && Equality_comparable<C, Val>()
248: Iterator<C> find(C& c, Val v)
249: {
250:     return std::find(c.begin(), c.end(), v);
251: }
252:
253: template<typename C, typename Pred>
254: // requires Container<C>() && Predicate<Pred, Value_type<C>>()
255: Iterator<C> find_if(C& c, Pred p)
256: {
257:     return std::find_if(c.begin(), c.end(), p);
258: }
259:
260: #endif //H112
```

```
1: //
2: //      Gundolf Haase, Oct 18 2024
3: //
4: #pragma once
5: #include <chrono>           // timing
6: #include <stack>
7:
8: //using Clock = std::chrono::system_clock;    //!< The wall clock timer chosen
9: using Clock = std::chrono::high_resolution_clock;
10: using TPoint= std::chrono::time_point<Clock>;
11:
12: // [Galowicz, C++17 STL Cookbook, p. 29]
13: inline
14: std::stack<TPoint> MyStopWatch; //!< starting time of stopwatch
15:
16: /** Starts stopwatch timer.
17:  * Use as @code tic(); myfunction(...) ; double tsec = toc(); @endcode
18:  *
19:  * The timing can be nested and the recent time point is stored on top of the stack.
20:  *
21:  * @return recent time point
22:  * @see toc
23:  */
24: inline auto tic()
25: {
26:     MyStopWatch.push(Clock::now());
27:     return MyStopWatch.top();
28: }
29:
30: /** Returns the elapsed time from stopwatch.
31:  *
32:  * The time point from top of the stack is used
33:  * if time point @p t_b is not passed as input parameter.
34:  * Use as @code tic(); myfunction(...) ; double tsec = toc(); @endcode
35:  * or as @code auto t_b = tic(); myfunction(...) ; double tsec = toc(t_b); @endcode
36:  * The last option is to be used in the case of
37:  * non-nested but overlapping time measurements.
38:  *
39:  * @param[in] t_b start time of some stop watch
40:  * @return elapsed time in seconds.
41:  *
42:  */
43: inline double toc(TPoint const &t_b = MyStopWatch.top())
44: {
45:     // https://en.cppreference.com/w/cpp/chrono/treat_as_floating_point
46:     using Unit = std::chrono::seconds;
47:     using FpSeconds = std::chrono::duration<double, Unit::period>;
48:     auto t_e = Clock::now();
49:     MyStopWatch.pop();
50:     return FpSeconds(t_e-t_b).count();
51: }
```