

# On the first law of genomics

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In 1998 on the conference *Microbial Genomes* Slonimski [1] formulated a law concerning the distribution of genes in a genome. Having several complete sequences of microbial genomes he divided genes into classes. He put into class  $n$  genes which appear exactly  $n$ -times in a genome. He observed that if  $x_n$  is a number of types of genes in a class  $n$  then

$$x_n \approx \frac{c}{2^n n}.$$

At the same time Huynen and Nimwegen [2] have compared the distribution of genes in eleven genomes and claim that  $x_n$  show power distribution. Recently, Koonin's group has published a few papers (e.g. [3], [4]) where they developed a simple model of this phenomena. In my talk I am going to present some general model in which we do not assume that the number of genes of a given type is bounded. The model is described by a system of infinite number of ordinary differential equations. We analyse asymptotic properties of the distribution of numbers of classes. We also compare theoretical results with the previous empirical studies. Our model rather justifies the Slominski's conjecture than that of Huynen and Nimwegen.

## References

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